

# Performance Contracting in After-Sales Service Supply Chains\*

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## Abstract

Performance-based contracting is reshaping service support supply chains in capital intensive industries such as aerospace and defense. Known as Power by the Hour in the private sector and as Performance-Based Logistics (PBL) in defense contracting, it aims to replace traditionally used fixed-price and cost-plus contracts in order to improve product availability and reduce the cost of ownership by tying a supplier’s compensation to the output value of the product generated by the customer (buyer).

To analyze implications of performance-based relationships, we introduce a multitask principal-agent model to support resource allocation and use it to analyze commonly observed contracts. In our model the customer (principal) faces a product availability requirement for the “uptime” of the end product. The customer then offers contracts contingent on availability to  $n$  suppliers (agents) of the key subsystems used in the product, who in turn exert cost reduction efforts and set spare parts inventory investment levels. We show that the first-best solution can be achieved if channel members are risk-neutral. When channel members are risk-averse, we find that the second-best contract combines a fixed payment, a cost-sharing incentive, and a performance incentive. Furthermore, we study how these contracts evolve over the product deployment life cycle as uncertainty in support cost changes. Finally, we illustrate the application of our model to a problem based on aircraft maintenance data and show how the allocation of performance requirements and contractual terms change under various environmental assumptions.

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# 1 Introduction

Support and maintenance services continue to constitute a significant part of the U.S. economy, often generating twice as much profit as do sales of original products. For example, a 2003 study by Accenture (see [1]) found that \$9B in after-sales revenues produced \$2B in profits for General Motors, which is a much higher rate of profit than its \$150B in car sales generated over the same time period. According to the same study, after-sales services and parts contribute only 25% of revenues across all manufacturing companies but are responsible for 40-50% of profits.

Since after-sales support services are often provided and consumed by two different organizations (i.e., the OEM and the customer), the issue of contracting between them becomes important. While contracts for maintenance services of simpler products (electronics, automobiles) involve fixed payments for warranties, there are many instances of complex systems that require more sophisticated relationships between service buyers and suppliers. For example, in capital-intensive industries such as aerospace and defense, significant uncertainties in cost and repair processes make it very hard to guarantee a predetermined service level or quote a price for providing it. Therefore maintenance support in these industries typically involves cost-sharing arrangements, which include fixed-price and cost-plus contracts. Under the former, the buyer of support services (henceforth called “customer”) pays a fixed fee to the supplier to purchase necessary parts and support services; under the latter, the customer compensates the supplier’s full cost and adds a premium.

Through our work with aerospace and defense contractors we have observed a major shift in support and maintenance logistics for complex systems over the past few years. Performance-based contracting, a novel approach in this area, is replacing traditional service procurement practices. This approach is often referred to as Power by the Hour or Performance-Based Logistics (PBL) in, respectively, the commercial airline and defense industries. The premise behind performance-based contracting is summarized in the official Department of Defense (DoD) guidelines (Section 5.3 in [12]): “The essence of Performance Based Logistics is buying performance outcomes, not the individual parts and repair actions... Instead of buying set levels of spares, repairs, tools, and data, the new focus is on buying a predetermined level of availability to meet the [customer’s] objectives.” In 2003, the DoD issued Directive 5000.1 [10] which “*requires* program managers to develop and implement PBL strategies that optimize total system availability.” Hence, all future DoD maintenance contracts are mandated to be performance-based.

A critical element of performance-based contracting is the clear separation between the customer’s expectations of service (the performance goal) and the supplier’s implementation (how it is achieved). In the words of Macfarlan and Mansir [22], “The contract explicitly identifies what is required, but the contractor determines how to fulfill the requirement.” As a consequence of this flexibility, PBL contracting should promote new and improved ways to manage spare parts inventory and reduce administrative overhead, negotiate contracts, and make resource allocation decisions. For example, under the traditional cost-plus contract, the supplier of a service must truthfully report its detailed cost structure to the customer in order to determine which expenses are eligible for reimbursement. Under a PBL arrangement, the supplier does not have to share cost information at this level of detail. Moreover, the customer no longer directly manages or possibly even owns resources such as the inventory of spares. Finally, in the long run suppliers may find it in their interest to invest in designing more reliable products and more efficient repair and logistics capabilities.

Not surprisingly, such a radical change in the approach to contracting has caused confusion among suppliers of after-sales support services. The academic literature, however, offers little guidance with respect to how such contracts should be executed. In this paper we aim to take a first step towards filling this void by proposing a model of performance-based contractual relationships that arise in practice when procuring repair and maintenance services. We embed a classical single-location spare parts inventory management problem into a principal-agent model with one principal (representing the end customer) and multiple interdependent agents (representing suppliers of the key product subsystems). Each agent performs two tasks that are subject to moral hazard: spare parts inventory management and cost reduction. We use this model to analyze three types of contracts (and any combination thereof) that are commonly encountered in aerospace and defense procurement and high technology industries, namely, fixed-price, cost-plus, and PBL. In analyzing these contracts we ask the following questions. (1) What is the optimal combination of contractual levers that achieves the best possible outcome for the customer? (2) How should a performance requirement for the final product be translated into the performance requirements for the suppliers who provide critical components? (3) How should the risk associated with the maintenance of complex equipment be shared among all supply chain members?

We show that, if suppliers’ decisions are observable and contractible, the contract that achieves the first-best solution is a nonperformance arrangement that combines partial cost reimbursement with a fixed payment. If supplier actions are unobservable and the parties are risk-neutral, we show that the first-best solution can still be achieved using a contract that combines a performance incentive with a

fixed payment (but no cost sharing). However, when even one of the parties is risk-averse, the first-best solution cannot be achieved. In this case, we show that “pure” fixed-price, cost-plus, or performance-based contracts (or any pair-wise combination of them) are not suitable because they do not provide the necessary incentives. Thus, we show that the second-best contract involves all three elements: a combination of a fixed payment, a cost sharing payment, and a performance-based payment. For any such contract proposed by the customer, we find analytically optimal decisions for all suppliers. Unfortunately, the customer’s problem neither is well-behaved nor admits tractable analytical solutions (the latter is true even in the centralized supply chain). Using a combination of analytical results for special cases and numerical analysis performed on a data set that is representative of a supply chain supporting a fleet of military airplanes, we obtain insights into the structure of the optimal contract. In particular, we study the sensitivity of the optimal contract to cost uncertainty and infer that, when the customer is less (more) risk-averse than the suppliers, the performance incentive increases (decreases) while the cost sharing incentive decreases (increases) as time progresses. Finally, we analyze the impact of problem parameters on contractual terms, performance, and profitability.

To the best of our knowledge, this paper represents the first attempt to embed the after-sales service supply chain model into the principal-agent framework in which the supply chain members behave in a self-interested manner. Our results are consistent with the observed practice of using multiple contract types whose mix evolves over time. The rest of the paper is organized as follows. After a brief review of related literature in Section 2, we present modeling assumptions and notations in Section 3. In Section 4 we analyze the first-best solution as well as derive solutions for the general second-best case. In Section 5 we analyze special cases, beginning with the risk-neutral case, then we study an environment in which the suppliers’ actions are partially observable, and finally we study a situation with one supplier. A numerical example that is based on the aforementioned military aircraft data set is presented in Section 6. Finally, in Section 7 we discuss managerial implications of our study.

## **2 Literature Review**

Two distinct models are blended together in our paper: a classical inventory planning model for repairable items, well known in operations management, and the moral hazard model that has been an area of active research in economics. The theory of repairable parts inventory management dates back to the 1960s when Feeney and Sherbrooke [14] introduced a stochastic model of the repairable inven-

tory problem whose steady-state solution relies on the application of Palm’s Theorem. Sherbrooke’s METRIC model (Sherbrooke [29]) established the basic modeling framework and heuristic optimization algorithms for allocating inventory resources in multi-echelon, multi-indentured environments. Subsequent models have led to notable success in enabling the management of multimillion-dollar service parts inventory resources in both commercial and government applications (e.g., see Cohen et al. [7] for a discussion of a successful application of multi-echelon optimization by IBM’s service support division). Research in this area has largely focused on improving computational efficiency and on incorporating more realistic modeling assumptions, such as allowing for capacitated supply or nonstationary demand processes. For a recent comprehensive account of developments in this field, see Muckstadt [25], who reviews the underlying theory, Sherbrooke [30], which focuses on aerospace and defense industry applications, and Cohen et al. [6], which introduces a modeling framework that has been used to guide the development of state-of-the art software solutions in various industries.

In brief, repairable inventory models are concerned with finding optimal (cost-minimizing) inventory stocking targets for each product component subject to a predefined service constraint. Service (performance) requirement can be defined in terms of either item fill rates or end product availability (i.e., system “uptime”). The latter is the preferred choice in aerospace and defense environments, and we adopt it in our paper (for a discussion of comparison of these metrics, see Sherbrooke [29]).

Numerous papers study the principal-agent models, and a comprehensive review can be found in Bolton and Dewatripont [2]. The building block for our paper is the moral hazard model in which actions of agents (suppliers) are unobservable to the principal (customer). Moreover, our model includes elements of multitasking (Holmström and Milgrom [15]), because the two decision variables for suppliers (the cost reduction effort and the inventory position) interact with each other. An additional complication is the presence of multiple agents whose decisions together impact the performance constraint that the principal faces. A number of economics papers discuss cost reimbursement contracts in the presence of moral hazard. For example, Scherer [28] considers optimal cost-sharing and the impact of risk aversion in defense procurement. McAfee and McMillan [24] presents a model in which firms bid for government contracts under significant cost-related risks. Inspired by this research, we allow for risk aversion and study cost-plus and fixed-price contracts in the context of after-sales support and compare them with performance-based contracts. In the operations management literature, a work by So and Tang [31] is closely related to our paper in that they also consider outcome-based reimbursement policies, but their focus is on the health-care industry.

Incentive alignment in supply chains through contracts has been a topic of great interest in operations management over the past decade (see Cachon [3] for a comprehensive survey). Recently, the role of information asymmetry has received considerable attention both in the adverse selection setting (representative articles include Corbett [8], Iyer et al. [16], Lutze and Ozer [21] and Su and Zenios [32]) and in the moral hazard setting (for example, see Plambeck and Zenios [27], Chen [4] and Plambeck and Taylor [26]). The current paper contributes to this growing area as well.

As is evident from our survey, the voluminous literature to date on repairable inventory management has been confined to single-firm models and hence does not address issues that arise in decentralized supply chains. Furthermore, although the extensive literature in economics aims to model contractual relationships among different parties, it does not address the complexities of repair and maintenance contracting environments. To our knowledge, our paper is the first to put a repairable inventory model into the decentralized framework and to study the issue of contracting in after-sales service supply chains.

### 3 Modeling Assumptions

The principal is the customer for  $N$  identical assembled products (“systems,” which can be airplanes, computers, manufacturing equipment, etc.) Each system is composed of  $n$  distinct major parts (“subsystems” which, in the case of an airplane, can represent avionics, engines, landing gear, weapons systems, etc.), each produced and maintained by a unique supplier. We use subscript 0 to denote the customer and subscript  $i$  for subsystem supplier  $i$ ,  $i = 1, 2, \dots, n$ . We ignore the indenture structure in the subsystem’s bill of materials, treating each subsystem as a single composite item. In the following subsections, we describe the repair process and supplier cost structure, explain how risk aversion is represented, define the performance measure, specify contract terms, and derive the utilities of the customer and the suppliers.

#### 3.1 Repair Process

Failure of the subsystem  $i$  is assumed to occur at a Poisson rate  $\lambda_i$ , independently from failures of other subsystems. Each supplier maintains an inventory of spares and a repair facility. A one-for-one base stock policy is employed for spares inventory control. That is, a failed unit is immediately replaced by a working unit (if it is available) from the supplier’s inventory. If a replacement is unavailable, a

backorder occurs, and the affected system becomes inoperable. As a result, downtime in any subsystem leads to downtime of the system. Upon failure, the defective unit immediately enters the repair facility, modeled as an M/G/ $\infty$  queue. We assume ample capacity (i.e., infinite number of servers) which is an idealization of reality, but it is considered a reasonable approximation in many circumstances (Sherbrooke [30]). This assumption leads to the desirable property that repair lead times of different items are independent. It takes, on average,  $L_i$  time units to repair the subsystem, and once the task is completed the subsystem is placed in the supplier's inventory. Forward and return transportation lead times are incorporated into the repair lead time and are assumed to be independent of the customer location (Wang et al. [34] relax this assumption).

The number of backorders of subsystem  $i$ ,  $B_i$ , is a random variable that is observed at a random point in time after steady state is reached. Supplier  $i$  chooses a target spare stocking level  $s_i$  for subsystem  $i$ .  $B_i$  and  $s_i$  are related to each other through  $B_i = (O_i - s_i)^+$ , where  $O_i$  is a stationary random variable representing the repair pipeline (on-order) inventory. Palm's Theorem states that  $O_i$  is Poisson-distributed for any repair lead time distribution, with the mean  $\mu_i \equiv \lambda_i L_i$  (Feeney and Sherbrooke [14]).

The repair process forms a closed-loop cycle. As the subsystems are typically very expensive and their lifetimes are very long, we assume that no subsystem is discarded during the entire support period. Figure 1 illustrates this process. Thus there are a total of  $N + s_i$  units of subsystem  $i$  in the supply chain, but only  $s_i$  of them are owned by the supplier. The fixed failure rate assumption is in fact an approximation, as the closed-loop cycle with finite population means  $\lambda_i$  is a function of the number of working units. However, this approximation is reasonable in our problem context because the condition  $E[B_i | s_i] \leq \lambda_i L_i \ll N$  is satisfied in practice for most spare subsystems. This condition ensures that, on average, the number of subsystems being repaired at any given time is relatively small, and the correction due to state-dependency can be safely ignored.

Although the Poisson distribution arising from Palm's Theorem is appealing, working with integer-valued random variables  $O_i$  and  $B_i$  as well as the discrete decision variable  $s_i$  significantly complicates our analysis of game-theoretic situations associated with various contracting options. In particular, deriving tractable mathematical expressions to gain insights into firms' behavior becomes prohibitively complex. For this reason, we depart from the usual discrete distribution assumption and model  $O_i$ ,  $B_i$ , and  $s_i$  as continuous variables. This approach is reasonable in our context since each unit of a supplier's inventory represents a composite of the various components associated with their particular

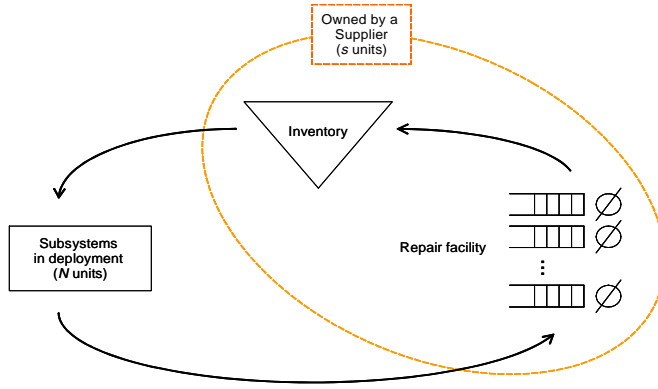


Figure 1: Closed loop cycle for repairable items.

subsystem. Such aggregation results in sufficiently high values for  $\mu_i$  so that normal approximation for the Poisson distribution can be applied (see Table 2 for a range of  $\mu_i$  used in a numerical example presented in Section 6). However, the normality assumption is not essential: we derive all our results for an arbitrary distribution. To this end, we let  $O_i$  be distributed continuously with cdf  $F_i$  and pdf  $f_i$ , which have nonnegative support  $[0, \infty)$  and  $F_i(0) \geq 0$ . The distribution of  $B_i$  is obtained from  $\Pr(B_i \leq x | s_i) = \Pr(O_i \leq x + s_i)$ . Furthermore,  $E[B_i | s_i] = \int_{s_i}^{\infty} [1 - F_i(x)] dx$  so we obtain

$$dE[B_i | s_i]/ds_i = -1 + F_i(s_i) \leq 0, \quad d^2E[B_i | s_i]/ds_i^2 = f_i(s_i) \geq 0. \quad (1)$$

Hence, we see that the expected backorder is decreasing and convex in  $s_i$ .

### 3.2 Supplier Cost

Supplier  $i$ 's total cost to maintain its subsystem,  $C_i$ , has fixed and variable components. The fixed cost contains an additive stochastic term  $\varepsilon_i$  having zero mean and finite variance. The expected fixed cost can be normalized to zero without affecting any of our results because it does not play a role in determining optimal supplier decisions and contract terms, as will become evident in the next section. The variable cost is equal to  $c_i$ , the unit cost of a spare subsystem, times  $s_i$ , the number of units in the base stock.  $\varepsilon_i$  represents the uncertainty in total cost that is beyond supplier  $i$ 's control, and  $\{\varepsilon_i\}$  are assumed to be uncorrelated across suppliers, i.e.,  $\text{Cov}[\varepsilon_i, \varepsilon_j] = 0$  for  $i \neq j$ . Furthermore, we assume that  $\text{Cov}[\varepsilon_i, B_i] = \text{Cov}[\varepsilon_i, B_j] = 0$  holds for all  $i$  and  $j$ . The uncertainty in the unit cost  $c_i$  is assumed to be negligible compared to  $\varepsilon_i$ . This assumption is based on our discussions with practitioners who indicated that the uncertainty with respect to fixed costs is of greater importance during the support

stage. The unit cost uncertainty may be significant during the product development stage, but we do not model it in this paper. In addition, we assume that  $c_i$  and the distributions of  $\varepsilon_i$  and  $B_i$  are common knowledge.<sup>1</sup>

The fixed cost of support can be reduced by the dollar amount  $a_i$ , which is interpreted as the supplier's cost reduction effort. We assume that the variable cost is unaffected by  $a_i$ . Hence,  $C_i = c_i s_i - a_i + \varepsilon_i$ . By exerting effort the supplier incurs disutility  $\psi_i(a_i)$ , which is convex increasing ( $\psi'_i(a_i) > 0$ ,  $\psi''_i(a_i) > 0$ ), and  $\psi_i(0) = 0$ . As is the case for  $c_i$ , we assume that  $\psi_i(a_i)$  is known to the customer. Note that the supplier is not compensated for his disutility of effort  $\psi_i(a_i)$ . With this convention, we effectively assume that the effort  $a_i$  is the supplier's own discretionary decision and, hence, the customer does not subsidize the supplier's internal cost for it. In other words, the customer reimburses only the undisputable *direct* cost of maintenance that would withstand the scrutiny of a possible audit. In the sequel, we assume a quadratic functional form  $\psi_i(a_i) = k_i a_i^2 / 2$  with  $k_i > 0$ . This assumption generates compact expressions without fundamentally changing the insights of our model (see, for example, Chen [4]). We take the accounting convention that  $C_i$  is observable by the customer and is the basis of reimbursement (see Laffont and Tirole [20] p. 55).

The crucial distinction between the supplier's actions  $a_i$  and  $s_i$  is the way each variable contributes to the performance outcomes. The backorder function is influenced by  $s_i$  only, since  $B_i = (O_i - s_i)^+$ , while the total cost  $C_i = c_i s_i - a_i + \varepsilon_i$  is affected by both decision variables. This interaction creates asymmetry in how the suppliers' actions influence outcomes  $B_i$  and  $C_i$ . Raising  $a_i$  reduces the total cost but has no impact on availability, while raising  $s_i$  improves availability but incurs a higher cost. The latter is the classical cost-availability trade-off seen in repairable inventory models. We do not consider an alternative formulation, whereby supplier effort impacts product reliability and/or repair capabilities (thus impacting  $\lambda_i$  and  $L_i$ ).<sup>2</sup>

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<sup>1</sup>That the unit cost is known to the customer is plausible in the defense industry, as most of the current PBL contracts apply to existing subsystems whose unit cost had to be revealed under pre-PBL relationships. In traditional defense contracting, the DoD negotiates the price of a spare part or a subsystem based on the reported unit cost.

<sup>2</sup>Having fixed  $\lambda_i$  and  $L_i$  is a reasonable representation of reality in the defense industry. At present, most PBL contracts are awarded for existing systems whose subsystem specifications (hence reliability) and repair facilities (e.g., specialized equipment, tools) are already set and cannot be easily altered. Endogenizing reliability improvement is considered in Kim et al. [18]

### 3.3 Risk Aversion

We assume that all members of the supply chain are risk-averse with expected mean-variance utility

$$E[U_i(X)] = E[X] - r_i \text{Var}[X] / 2. \quad (2)$$

The constant  $r_i \geq 0$  is the risk aversion factor, representing member  $i$ 's inherent attitude towards uncertainty. Great uncertainties that pervade product development, production, and maintenance mean significant risks for the firms, and their risk-averse perspective is commonly observed (see Scherer [28] for discussion and references). The larger the value of  $r_i$ , the more risk-averse a firm is, whereas risk neutrality is a special case with  $r_i = 0$ . This form of utility function has been widely used in recent operations management literature because of its tractability (Chen and Federgruen [5], Van Mieghem [33]).

### 3.4 Performance Measure

The performance metric for supplier  $i$  in our problem is subsystem availability  $A_i = 1 - B_i/N$ , the fraction of deployed systems that have a functional subsystem  $i$  at a random point in time. Note that each backorder of subsystem  $i$  results in a downed system. Similarly, we define the system availability  $A_0$  as the fraction of deployed systems that are fully functional. One can see that  $1 - \sum_{i=1}^n B_i/N \leq A_0 \leq 1 - \max_i \{B_i\}/N$ . However, a common assumption in the literature (for example, see Muckstadt [25]) is that the probability of two or more subsystems being down within the same system at any point in time is negligible. This is a reasonable assumption in our case since the failures of deployed subsystems typically occur very infrequently. Thus, the relation  $A_0 = 1 - B_0/N$  where  $B_0 = \sum_{i=1}^n B_i$  is assumed to hold for our problem, and no ambiguity exists in assigning accountability for system downtime to a specific supplier.

Because of the one-to-one correspondence between  $A_0$  and  $B_0$  resulting from the assumption, the system availability requirement  $E[A_0 | s_1, s_2, \dots, s_n] \geq \hat{A}_0$  (e.g., “expected system availability has to exceed 95%”) is equivalent in our model to a system backorder constraint  $E[B_0 | s_1, s_2, \dots, s_n] = \sum_{i=1}^n E[B_i | s_i] \leq \hat{B}_0$ . We call  $\hat{B}_0$  the system backorder target. Additionally, we assume that  $\sum_{i=0}^n \mu_i > \hat{B}_0$  in order to rule out the trivial case in which  $s_1 = s_2 = \dots = s_n = 0$  is optimal.

We note that our focus on performance incentives raises the question of how our definition of subsystem availability can be used to quantify supplier performance. One approach would be to

compute the backorder metric as the time average of the stationary backorder process (indexed by time  $t$ ) and not the stationary variable itself. That is, the random variable  $\tilde{B}_i(\tau) \equiv \frac{1}{\tau} \int_0^\tau B_i(t) dt$  could be used, instead of  $B_i$ , as the performance metric.  $\tau$  is the horizon over which the number of backorders are counted and averaged. The distinction between these two measures is inconsequential in a risk-neutral setting since the utilities of the customer and the suppliers are functions of expectation only, and  $E[\tilde{B}_i(\tau)] = E[B_i]$ . For the case of risk aversion, however, these two measures diverge because  $\text{Var}[B_i | s_i]$  is independent of  $\tau$  while  $\text{Var}[\tilde{B}_i(\tau) | s_i]$  decreases with  $\tau$ . The latter is a consequence of the ergodic property of  $B_i(t)$ . Therefore, if we were to adopt  $\tilde{B}_i(\tau)$  as our performance measure, uncertainty with respect to availability may become insignificant with sufficiently large  $\tau$ . However, this is not a good representation of reality because the customer and the suppliers alike express major concerns about performance variability at any point of time rather than time-averaged performance. For example, The DoD Guide for Achieving Reliability, Availability, and Maintainability [11] defines availability as “a measure of a degree to which an item is in operable state and can be committed at the start of a mission when the mission is called for *at an unknown (random) point in time*”. In line with this definition, we choose availability defined in terms of steady state backorders as the appropriate performance measure.<sup>3</sup> We note, however, that there is an ongoing debate on this very issue among the practitioners in the aerospace and defense industries (see Kim et al. [17] for further details).

### 3.5 Contract Terms and Utilities

The customer’s payment (transfer) to the supplier  $i$  is comprised of three terms: (1) a fixed payment, (2) reimbursement for the supplier’s cost, and (3) a backorder-contingent incentive payment. Specifically, it has the form

$$T_i(C_i, B_i) = w_i + \alpha_i C_i - v_i B_i, \quad (3)$$

where  $w_i$ ,  $\alpha_i$ , and  $v_i$  are the contract parameters determined by the customer.  $w_i$  is the fixed payment,  $\alpha_i$  is the customer’s share of the supplier’s costs, and  $v_i$  is the penalty rate for backorders  $B_i$  incurred by the supplier. With  $v_i = 0$  and  $\alpha_i = 0$ , we obtain a fixed-price (FP) contract; with  $\alpha_i = 1$  and  $v_i = 0$  we obtain a cost-plus (C+) contract with full reimbursement.

Under the assumptions we have laid out so far, supplier  $i$  who is given a contract  $T_i(C_i, B_i)$  has the

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<sup>3</sup>For completeness, we have investigated the impact of choosing the alternative measure  $\tilde{B}_i(\tau)$  and found that none of the qualitative results in this paper change, except for numerical adjustments on the optimal contract parameters. See the accompanying Technical Appendix (Kim et al. [17]).

following expected utility:

$$E[U_i(T_i(C_i, B_i) - C_i) - \psi_i(a_i) | a_i, s_i] = w_i - (1 - \alpha_i)(c_i s_i - a_i) - v_i E[B_i | s_i] - k_i a_i^2 / 2 \quad (4)$$

$$- r_i (1 - \alpha_i)^2 \text{Var}[\varepsilon_i] / 2 - r_i v_i^2 \text{Var}[B_i | s_i] / 2.$$

The first three terms together represent the expected net income of the supplier, while the fourth term is internal disutility for exerting cost reduction effort. The last two terms, respectively, represent risk premiums associated with cost and performance uncertainties. Similarly, the customer's expected utility is

$$E[U_0(-\sum_{i=1}^n T_i(C_i, B_i)) | \{a_i, s_i\}] = -\sum_{i=1}^n (w_i + \alpha_i(c_i s_i - a_i) - v_i E[B_i | s_i]) \quad (5)$$

$$+ r_0 \alpha_i^2 \text{Var}[\varepsilon_i] / 2 + r_0 v_i^2 \text{Var}[B_i | s_i] / 2.$$

That is, the customer's utility is a function of her total expenditure only. Lastly, each supplier is assumed to have fixed reservation utility which he can gain by not participating in the trade with the customer. Without loss of generality, we can normalize its value to zero.

### 3.6 Sequence of Events

Our representation of the after-sales support relationship is based on the standard single-location, steady-state repairable model with a take-it-or-leave-it contract. We do not consider issues arising from repeated interactions between the customer and the suppliers in this paper.<sup>4</sup>

Under the assumptions of the model, the sequence of events is as follows. (1) the customer offers the suppliers take-it-or-leave-it contracts; (2) the suppliers accept or reject the contracts; (3) the suppliers who have accepted the contracts take cost reduction measures and set the base stock levels of their spares inventory; (4) realized costs and backorders are evaluated at the end of the contract horizon; and finally (5) suppliers are compensated according to the contract terms.

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<sup>4</sup>Due to uncertainties in fleet deployment schedules and future support budgets, the DoD is unwilling to sign long-term contracts (i.e., for the life of the program) and instead typically contracts on a shorter-term basis with annual adjustments. Suppliers typically conduct multi-period budget planning using a short-term, steady-state model on a rolling horizon basis. Therefore, making a single-interaction assumption is appropriate. Although pre-contractual bargaining or renegotiation may exist in practical situations, we do not formally model them in this paper.

## 4 Analysis

In the performance-based contracting environment, neither the details of supplier cost nor how the supplier meets their performance objectives is revealed to the customer. Instead, each supplier is compensated based on his total realized cost  $C_i$  and his realized backorder level  $B_i$ . The fact that both of these contractible variables include uncertainty raises the issue of incentives. Since  $C_i$  and  $B_i$  are functions of the supplier's cost reduction effort  $a_i$  and base stock level decision  $s_i$ , the supplier can partially control the performance related to his subsystem and his compensation by setting  $a_i$  and  $s_i$ . However, he may choose a pair  $(a_i, s_i)$  that is not optimal from the customer's point of view. For example, an opportunistic supplier may choose to minimize his own disutility of efforts by "shirking" (i.e., choosing low  $a_i$  and  $s_i$ ), hoping that a fortuitous state of the world is realized. The customer's task is then to provide appropriate incentives through contract terms that would induce the supplier to make the desired decisions. The customer's objective is to maximize her expected utility (or minimize her negative utility) subject to the system availability requirement, or equivalently, the backorder requirement. In the following discussion, we use the term "observable" to mean that a variable is both observable and verifiable and hence can be specified in a contract. We first present the benchmark case with complete observability and then consider the private action case. This section concludes with a comparison of common contracting options.

### 4.1 First-Best Solution: Complete Observability of Suppliers' Actions

In this subsection we analyze the problem under the assumption that suppliers' actions  $\{a_i, s_i\}$  are both observable, a situation often referred to as the first-best solution because the customer avoids incentive problems by dictating  $\{a_i, s_i\}$  to the suppliers. This is the benchmark case against which we can evaluate the efficiency of other contracts. The customer's problem is

$$\begin{aligned}
 (\mathcal{A}_{FB}) \quad & \min_{\{w_i, \alpha_i, v_i, a_i, s_i\}} E[U_0(\sum_{i=1}^n T_i(C_i, B_i)) | \{a_i, s_i\}], \\
 \text{s.t.} \quad & \sum_{i=1}^n E[B_i | s_i] \leq \widehat{B}_0, \tag{AR} \\
 & E[U_i(T_i(C_i, B_i) - C_i) - \psi_i(a_i) | a_i, s_i] \geq 0 \quad \forall i, \tag{IR}_i \\
 & 0 \leq \alpha_i \leq 1, \quad a_i, s_i \geq 0 \quad \forall i.
 \end{aligned}$$

The expected utility expressions are given by (4) and (5). (AR) is the system availability require-

ment constraint expressed in terms of backorders, and  $(\text{IR}_i)$  is the individual rationality constraint that ensures supplier  $i$ 's participation. As is typical in moral hazard problems, each  $(\text{IR}_i)$  constraint binds at the optimal solution. That is, the customer is able to extract all of the surplus from the suppliers by setting appropriate fixed payments  $\{w_i\}$ . Let  $\theta$  be the Lagrangian multiplier associated with the constraint (AR). The following proposition specifies the first-best solution.

**Proposition 1** *When the suppliers' decisions are observable and contractible, the optimal contract specifies the following supplier decisions  $(a_i, s_i)$ :*

$$a_i = 1/k_i, \quad (6)$$

$$s_i(\theta) = F_i^{-1}(\max\{1 - c_i/\theta, 0\}), \quad (7)$$

$$\sum_{i=1}^n E[B_i | s_i(\theta)] = \widehat{B}_0. \quad (8)$$

The solution  $\{a_i^{FB}\}$ ,  $\theta^{FB}$  and  $\{s_i^{FB}\} = \{s_i(\theta^{FB})\}$  is unique and is obtained by offering a non-performance-based, risk-sharing contract such that  $v_i^{FB} = 0$  and

$$\alpha_i^{FB} = r_i / (r_0 + r_i) \quad (9)$$

provided that  $r_0 > 0$  or  $r_i > 0$ . Supplier  $i$ 's expected utility is zero, whereas the customer's expected utility is  $\sum_{i=1}^n \left( -c_i s_i^{FB} + \frac{1}{2k_i} - \frac{1}{2} \frac{r_0 r_i \text{Var}[\varepsilon_i]}{r_0 + r_i} \right)$ .

We note that  $\{s_i^{FB}\}$  and  $\theta^{FB}$  are determined simultaneously from equations (7) and (8). The optimal risk sharing of cost, represented by (9), is a modified version of the Borch rule (see Bolton and Dewatripont [2]). To gain insights, we consider extreme cases. If  $r_0 > 0$  and  $r_i = 0$ , i.e., if supplier  $i$  is risk-neutral but the customer is not,  $\alpha_i = 0$ . This outcome corresponds to a FP contract; since the customer is risk-averse while the supplier is not, the customer transfers all risks to the supplier. At the opposite end, consider  $r_0 = 0$  but  $r_i > 0$ , i.e., only the customer is risk-neutral. In this case  $\alpha_i = 1$ , meaning that the C+ contract with full reimbursement is used. Although it may sound counterintuitive that the C+ contract achieves the first-best solution, we should recall that incentives are not an issue in the current setting because the suppliers' actions are observable and contractible. The role of the C+ contract is merely to mitigate the suppliers' reluctance to participate in the trade (the  $(\text{IR}_i)$  constraint). The risk-neutral customer can absorb all risks without efficiency loss. When

both  $r_0$  and  $r_i$  are positive, the customer and the supplier  $i$  share the risk according to (9), i.e., based on the supplier's risk aversion relative to that of the customer. For the remaining case  $r_0 = r_i = 0$  (which is not covered by Proposition 1), risk sharing is not an issue, and an infinite number of  $(w_i, \alpha_i, v_i)$  combinations are optimal.

We now focus on the customer's first-best expected utility, which contains three terms for each supplier. The first term  $(-c_i s_i^{FB})$  is the cost of owning  $s_i^{FB}$  units in the supplier's spares inventory. The second term  $1/2k_i$  is the net savings due to the supplier's cost reduction efforts. The last term  $\frac{1}{2} \frac{r_0 r_i}{r_0 + r_i} \text{Var}[\varepsilon_i]$  can be interpreted as the joint risk premium between supplier  $i$  and the customer, and it is positive only if they are both risk-averse. It represents the inefficiency created by a trade-off between the customer's desire to protect herself from risk and to facilitate the suppliers' participation, which require some degree of risk-sharing through cost reimbursement.

Unlike cost risk  $\text{Var}[\varepsilon_i]$ , performance risk  $\text{Var}[B_i | s_i]$  poses no trade-off between the customer and the suppliers; it can be eliminated by setting  $v_i = 0$ . In other words, all parties mutually benefit without the performance clause in the first-best case. If  $v_i > 0$ , a risk-averse supplier demands a premium due to the possible penalty associated with the stochastic realization of backorders. This leads to income fluctuations to a risk-averse customer. Both concerns disappear when  $v_i = 0$  without incurring extra cost because the contractibility of the suppliers' actions  $\{s_i\}$  implies that the actions can be perfectly enforced even without performance incentives. Thus, the customer's attitude toward cost uncertainty and performance uncertainty differ. This key observation will continue to hold even when the suppliers' actions are unobservable and, hence, not contractible.

## 4.2 Private Actions: The Suppliers' Problem

We now turn to the situation in which suppliers' actions are unobservable to the customer, as is expected in a PBL environment. Given the contract parameters  $(w_i, \alpha_i, v_i)$ , supplier  $i$  chooses  $(a_i, s_i)$  that maximize his expected utility (4). That is, he solves

$$\max_{a_i, s_i} w_i - (1 - \alpha_i)(c_i s_i - a_i) - v_i E[B_i | s_i] - k_i a_i^2 / 2 - r_i (1 - \alpha_i)^2 \text{Var}[\varepsilon_i] / 2 - r_i v_i^2 \text{Var}[B_i | s_i] / 2.$$

A distinctive feature of this problem is that  $\text{Var}[B_i | s_i]$  is a function of the decision variable  $s_i$ . This is a departure from most moral hazard models, in which, only the mean of the performance measure is affected by the decision variable. In our model the dependence of  $\text{Var}[B_i | s_i]$  on  $s_i$  is unavoidable.

As will become evident, this dependency complicates the analysis significantly but at the same time creates new dynamics. The supplier's problem is generally not quasiconcave in  $s_i$ , but unimodality can be guaranteed under mild parametric assumptions.

**Proposition 2** *Suppose  $\alpha_i < 1$  and  $v_i[1 - F(0)] \geq (1 - \alpha_i)c_i$ . Then there is a unique interior optimal solution to the supplier's problem in which supplier  $i$  chooses  $a_i^*$  and  $s_i^*$  such that*

$$a_i^* = (1 - \alpha_i) / k_i, \quad (10)$$

$$v_i[1 - F_i(s_i^*)] + r_i v_i^2 F_i(s_i^*) E[B_i | s_i^*] = (1 - \alpha_i)c_i. \quad (11)$$

The conditions we specify in Proposition 2 ensure that the supplier's utility function is increasing at  $s_i = 0$ . These conditions depend on  $\alpha_i$  and  $v_i$ , which are determined by the customer (optimal solutions for these are presented in the next subsection). We have verified through numerical examples that the conditions are mild in the sense that they violated only under extreme parameter settings (e.g., when the customer's risk aversion factor  $r_0$  is orders of magnitude greater than that of the supplier,  $r_i$ ). We henceforth assume that the conditions of Proposition 2 are always satisfied. From the proposition we obtain the following results, which offer insights into the impact of contract parameters on optimal decisions.

**Corollary 1** *Suppose the conditions in Proposition 2 hold. Then*

- (i)  $\partial s_i^* / \partial r_i > 0$ ,  $\partial a_i^* / \partial r_i = 0$ ,
- (ii)  $\partial s_i^* / \partial \alpha_i > 0$ ,  $\partial a_i^* / \partial \alpha_i < 0$ , and
- (iii)  $\partial s_i^* / \partial v_i > 0$ ,  $\partial a_i^* / \partial v_i = 0$ .

From (i) we see that the more risk-averse the supplier, the greater the optimal inventory position he chooses. By investing in more spares, the supplier reduces the likelihood of backorder occurrences, thereby reducing the variance associated with performance. Hence, increasing  $s_i$  is a preventive measure that can be taken by the supplier to avoid performance risk. A similar mechanism, however, does not exist for avoiding cost risk, as evidenced by the fact that the optimal cost reduction effort  $a_i^*$  is independent of the degree of risk aversion  $r_i$  (see equation (10)).<sup>5</sup>

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<sup>5</sup>This result is due to the assumption that the stochastic term  $\varepsilon_i$  enters additively into the supplier's total cost  $C_i = c_i s_i - a_i + \varepsilon_i$ ; the effort reduces the mean of  $C_i$  but not the variance. Under this standard assumption the supplier has no control over the variability of cost, so his attitude toward risk does not factor into the decision about  $a_i^*$ .

Parts (ii) and (iii) of Corollary 1 explain optimal supplier responses to the contract terms  $\alpha_i$  and  $v_i$ . If the customer increases the reimbursement ratio  $\alpha_i$ , the supplier becomes less concerned with cost overruns and hence does not exert as much cost reduction effort as he might otherwise ( $\partial a_i^*/\partial \alpha_i < 0$ ). At the same time, his perceived *effective* unit cost of inventory ( $(1 - \alpha_i)c_i$  on the right-hand side of (11)) decreases, making it desirable to stock more. With respect to the backorder penalty  $v_i$ , a larger  $v_i$  means a stronger incentive to decrease backorders so  $s_i^*$  increases. However,  $v_i$  does not affect  $a_i^*$ , as it serves only as an incentive to reduce backorders and not the total cost. This behavior is, in part, a consequence of our modeling assumptions that the supplier's effort  $a_i$  affects only the cost and that the uncertainties in cost and in performance are independent of each other.

### 4.3 Private Actions: The Customer's Problem

Anticipating that the suppliers will respond by choosing  $\{a_i, s_i\}$  according to (10) and (11), the customer selects contract terms  $\{w_i, \alpha_i, v_i\}$  that achieve minimal total disutility subject to the backorder constraint. With the right incentives, each supplier will voluntarily choose  $(a_i, s_i)$  that match the customer's expectation, even though the suppliers' decisions are not directly verified. This voluntary action is expressed in terms of incentive compatibility (IC) constraints

$$(a_i^*, s_i^*) \in \arg \max E [U_i (T_i(C_i, B_i) - C_i - \psi_i(a_i)) \mid a_i, s_i \geq 0] \quad \forall i. \quad (\text{IC}_i)$$

The customer's problem formulation is similar to  $(\mathcal{A}_{FB})$ , except that the contract space is reduced to  $\{w_i, \alpha_i, v_i\}$  as  $\{a_i^*, s_i^*\}$  are now determined by those terms, and that  $(\text{IC}_i)$  constraints are added. As in the first-best case, it can be demonstrated that the  $(\text{IR}_i)$  constraints bind at the optimum, so that we can simplify the problem by solving for values of  $\{w_i\}$  that leave the suppliers with zero expected utility. Using the Lagrange multiplier  $\theta$  for the backorder constraint (AR), we can write  $n$  individual Lagrangian functions. Moreover, it is convenient to convert the Lagrangian into a function of  $(\alpha_i, s_i, \theta)$  rather than a function of  $(\alpha_i, v_i, \theta)$ , using the monotonicity result  $\partial s_i^*/\partial v_i > 0$  from Corollary 1. Using (10), we obtain

$$\begin{aligned} \mathcal{L}_i(\alpha_i, s_i, \theta) &= c_i s_i + \theta E [B_i \mid s_i] - (1 - \alpha_i)/k_i + (1 - \alpha_i)^2 / (2k_i) + (r_0 \alpha_i^2 + r_i (1 - \alpha_i)^2) \text{Var}[\varepsilon_i] / 2 \\ &\quad + (r_0 + r_i) [v_i(\alpha_i, s_i)]^2 \text{Var}[B_i \mid s_i] / 2, \end{aligned} \quad (12)$$

whereby

$$v_i(\alpha_i, s_i) = \begin{cases} \frac{(1-\alpha_i)c_i}{1-F_i(s_i)} & \text{if } r_i = 0, \\ \frac{1-F_i(s_i)}{2r_i F_i(s_i) E[B_i | s_i]} \left( -1 + \sqrt{1 + \frac{4r_i c_i (1-\alpha_i) F_i(s_i) E[B_i | s_i]}{[1-F_i(s_i)]^2}} \right) & \text{if } r_i > 0, \end{cases} \quad (13)$$

from (11). We readily notice that the optimal performance incentive  $v_i(\alpha_i, s_i)$  is a decreasing function of  $\alpha_i$ ; in order to have the supplier choose  $s_i$ , the customer may decrease  $v_i$  while increasing  $\alpha_i$ , or vice versa. Thus,  $v_i$ , the incentive to increase the stocking level, and  $1 - \alpha_i$ , the incentive to reduce costs, are complements. This observation plays a key role in a later analysis and will be discussed further.

We denote the optimal solution pairs with superscripts  $SB$ ,  $\{\alpha_i^{SB}, s_i^{SB}\}$ . Unfortunately, (12) is not generally quasiconvex and hence is not necessarily unimodal. The analytical specification of  $s_i^{SB}$  is intractable even with  $\alpha_i$  fixed, thereby requiring numerical analysis. To gain additional insights while circumventing this difficulty, in the next section we focus on several special cases and later analyze the original problem numerically.

#### 4.4 Cost Plus (C+) vs. Fixed Price (FP) vs. Performance-Based Contracts

Before delving into the analysis of optimal contracts for special cases, we pause here to evaluate the effectiveness of the most widely used contract forms, C+ ( $\alpha_i = 1, v_i = 0$ ) and FP ( $\alpha_i = v_i = 0$ ), and compare them with performance contracts ( $v_i > 0$ ). Consistent with other literature analyzing and comparing these contracts (see, for example, Scherer [28]), our model indicates that C+ and FP are polar opposites when it comes to providing cost reduction incentives. With a FP contract a supplier becomes the residual claimant and, hence, it is in his interest to reduce costs as much as possible. In terms of cost risk, the FP contract gives perfect insurance to the customer because the supplier bears all risks from cost under- or overruns. In contrast, the C+ contract shifts all risks to the customer, as she has to reimburse whatever the supplier's realized cost may be. At the same time, the C+ contract provides no incentive for the supplier to reduce costs.

Despite the prevalence of C+ and FP contracts in practice, they do not induce the desired supplier behavior when a performance constraint is present and the customer cannot observe suppliers' actions. This becomes clear after inspecting the supplier's utility function (4). With the FP contract, it is in the supplier's interest to reduce not only effort  $a_i$  but also spares inventory  $s_i$  as much as possible, thus violating the minimum availability desired by the customer. A C+ contract, on the other hand, has the

Contract type	No performance-based compensation ( $v = 0$ )	Performance-based compensation ( $v > 0$ )
<b>Pure performance</b> ( $\alpha = 0, w = vN$ )		The customer is unable to extract all supplier surplus.
<b>Fixed price</b> ( $\alpha = 0$ )	While achieving the first-best cost reduction effort $a^{FB}$ , the supplier is incentivized to reduce $s$ as much as possible.	First-best can be achieved with the appropriate choice of $w$ and $v$ under risk neutrality. First-best is not achieved under risk aversion ( $\alpha > 0$ ) in general.
<b>Cost plus</b> ( $\alpha = 1$ )	The supplier exerts no cost reduction effort ( $a = 0$ ) and is indifferent toward $s$ .	The supplier exerts no cost reduction effort ( $a = 0$ ) and tries to increase $s$ as much as possible.

Table 1: Incentive effects of various contract combinations.

effect of making the supplier indifferent to the choice of  $s_i$ . Clearly, inducing proper actions requires performance incentives. The simplest contract in this category (the “pure performance contract”) has  $\alpha_i = 0$  and  $w_i = v_i N$  with  $v_i > 0$ . By setting  $w_i = v_i N$ , the payment to supplier  $i$  becomes  $T_i = v_i N(1 - B_i/N) = v_i N A_i$ , so in this case  $v_i$  is interpreted as the price for a percent of availability that the supplier is able to provide to each deployed system. Indeed, such a contract can induce the supplier to choose the optimal inventory level  $s_i$ . But it is inefficient because it leaves a positive residual surplus to the suppliers (i.e., the (IR) constraint does not bind in general). Interestingly (to be demonstrated in the following section), a contract with  $w_i > 0$  and  $v_i > 0$  that are determined independently can achieve the first-best solution if all parties are risk-neutral. However, proper risk sharing requires  $\alpha_i > 0$ , so the optimal contract will have all three components: a fixed payment, a cost-sharing clause, and a performance incentive. Table 1 summarizes supplier behavior under all of these contract combinations.

## 5 Special Cases

### 5.1 Risk-Neutral Firms

Many difficulties associated with the analysis disappear if all suppliers and the customer are risk-neutral, which may be the case in practice if the customer and the suppliers are all very large, well-diversified corporations. In this case, as we show below, even when actions are unobservable, the first-best solution is achieved with a contract that is a simple combination of a fixed payment and a performance component (henceforth called FP/performance). This solution highlights the performance allocation aspect of our problem at the expense of ignoring the issue of risk-sharing.

**Proposition 3** *With  $r_0 = r_1 = \dots = r_n = 0$ , the first-best solution is achieved if and only if*

- (i)  $\alpha_1 = \alpha_2 = \dots = \alpha_n = 0$ ,
- (ii)  $w_i = c_i s_i^{FB} + \theta^{FB} E[B_i | s_i^{FB}] - 1/2k_i$ ,
- (iii)  $v_1 = v_2 = \dots = v_n = \theta^{FB}$ ,

where  $\{s_i^{FB}\}$  and  $\theta^{FB}$  are computed from (7) and (8). The supplier  $i$ 's expected utility is zero, while the customer's expected utility is  $\sum_{i=1}^n (-c_i s_i^{FB} + 1/2k_i)$ .

The preceding result is not entirely new: it is often the case in other principal-agent models that the first-best solution is achieved with an FP/performance contract between two risk-neutral firms when there is only one effort variable (for example, see Bolton and Dewatripont [2]). Having two effort variables  $a_i$  and  $s_i$  as well as multiple suppliers does not change this basic result. First-best is obtained because  $\alpha_i$  and  $v_i$  under risk neutrality serve only as incentives and not as instruments for providing insurance against risk, eliminating the trade-off between the two factors.

An interesting deviation from the classical analysis involves just one supplier. It is captured in part (iii), which can be interpreted to mean that every backorder from heterogeneous subsystems has equal importance regardless of the subsystem unit price  $c_i$ . Thus, performance incentives are equal across suppliers. In our additively separable backorder model ( $B_0 = \sum_{i=1}^n B_i$ ) this makes intuitive sense, because the customer does not discriminate between a backorder of a \$1,000 item and that of a \$10 item; each item contributes equally to the downtime of the system. However, it would be erroneous to conclude that item unit costs  $\{c_i\}$  have no effect on determining the uniform performance incentive  $v_1 = \dots = v_n = \theta^{FB}$  because they determine  $\theta^{FB}$  indirectly through the joint satisfaction of (7) and (8). The fact that penalty rates are linked across suppliers continues to hold in the risk-averse case, although the equality as in (iii) can no longer be sustained because of the suppliers' varying attitudes toward risk. The policy implication of this result is to treat all suppliers equally with respect to the performance incentive as long as risk aversion is not present.

## 5.2 Risk-Averse Firms: Cases with Partial Observability

As the next step in gaining insights we now analyze the problem under a simplifying assumption that either  $\{s_i\}$  or  $\{a_i\}$  are observable and contractible, but not both. As will become evident, these special cases serve as bounds on the optimal contract parameters under conditions of complete unobservability and hence are useful in understanding the structure of the problem. We shall first consider the case

when  $\{s_i\}$  are observable but  $\{a_i\}$  are not. This may happen if the suppliers utilize consignment inventory management for all subsystems (which is sometimes the case in practice) so that inventories are visible to the customer. As  $s_i$  can now be dictated by the customer, the performance incentive  $v_i$  is unnecessary, i.e., the optimal contract has  $v_i = 0$  for all  $i$ . The optimal contract (denoted by the superscript  $SO$ ) is as follows.

**Proposition 4** *When  $\{s_i\}$  of all suppliers are observable to the customer but  $\{a_i\}$  are not, it is optimal for the customer to specify the contract terms according to*

- (i)  $\alpha_i^{SO} = k_i r_i / (1/\text{Var}[\varepsilon_i] + k_i(r_0 + r_i)) < \alpha_i^{FB}$ ,
- (ii)  $w_i^{SO} = (1 - \alpha_i^{SO})c_i s_i^{FB} - (1 - \alpha_i^{SO})^2 / (2k_i) + r_i(1 - \alpha_i^{SO})^2 \text{Var}[\varepsilon_i] / 2$ , and
- (iii)  $v_i^{SO} = 0$ .

$s_i^{SO} = s_i^{FB}$  is imposed on supplier  $i$  while the contract terms induce the cost reduction effort  $a_i^{SO} = (1 + k_i r_0 \text{Var}[\varepsilon_i]) / (k_i + k_i^2(r_0 + r_i) \text{Var}[\varepsilon_i])$ .

Even though one of the supplier's actions is observable to the customer, we see that the first-best solution cannot be achieved and, hence, incentive issues create inefficiencies. Namely, cost sharing is less than the optimal under the first-best solution ( $\alpha_i^{SO} < \alpha_i^{FB}$ ). The customer has to provide more incentive to reduce costs than would have been the case if she dictated  $a_i$ , and this is achieved by exposing the supplier  $i$  to more risk (smaller  $\alpha_i$ ). We see that  $\alpha_i^{SO}$  exhibits intuitive properties: as  $\text{Var}[\varepsilon_i]$  approaches infinity,  $\alpha_i^{SO}$  increases asymptotically to the first-best optimal risk sharing ratio  $\alpha_i^{FB}$  because the supplier's effort  $a_i$  becomes overshadowed by huge cost uncertainty. It is also clear that  $\alpha_i^{SO}$  moves toward zero (toward an FP contract) as  $\text{Var}[\varepsilon_i]$  decreases. The relative risk aversion ratio  $r_0/r_i$  is another major determinant of  $\alpha_i^{SO}$  which is similar to the first-best case. If the ratio is small,  $\alpha_i^{SO}$  is on the C+ side (closer to 1) whereas a large ratio implies that  $\alpha_i^{SO}$  is on the FP side (closer to 0).

The other possibility is when  $\{a_i\}$  of all suppliers are observable but  $\{s_i\}$  are not. This situation could arise in government contracting where a significant amount of information on supplier costs must be divulged to the customer.<sup>6</sup> We denote the optimal solution in this case with the superscript  $AO$ . It is easy to show that  $a_i^{AO} = a_i^{FB}$  as in (6), but tractable expressions for  $\alpha_i^{AO}$  and  $s_i^{AO}$  do not exist.

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<sup>6</sup>The Truth in Negotiations Act (TINA) has been applied to many government contracts since the 1960's. It requires suppliers to reveal cost data to the government (customer) in order to avoid excessive payments to the suppliers. In most PBL contracts, however, TINA is waived.

Despite this shortcoming,  $\alpha_i^{AO}$  can be evaluated analytically in the special case with only one supplier, a scenario we present next.

### 5.3 Single Risk-Averse Supplier

In this subsection we assume that there is only one supplier, so we drop the subscript  $i$ . Not only is such a firm-to-firm setting consistent with a majority of supply chain contracting models in the literature, but it is also a commonly observed situation in PBL practice. For example, a setting in which maintenance of a single key component is outsourced or a military customer contracts directly with a subsystem supplier fits this description (e.g., the U.S. Navy’s PBL contract with Michelin for tires or commercial airline Power by the Hour contracts with engine manufacturers like GE and Rolls Royce). As we will see shortly through numerical experiments, insights from this simpler model continue to hold for the general assembly structure with multiple suppliers.

With a single supplier, it may appear that the customer should set incentives so that  $E[B | s^{SB}] = \widehat{B}_0$  holds. In particular, this would be the case if the customer’s objective function were increasing monotonically in  $s$ , which is an intuitive property. Unfortunately, this intuition is not entirely correct. As noted in the previous section, the analysis of risk-averse firms is complicated by the non-quasiconcavity, implying that the Lagrangian (12) can be bimodal. Thus, the customer may prefer for the supplier to have more inventory than follows from  $E[B | s^{SB}] = \widehat{B}_0$ . This, however, happens only in extreme cases in which the customer is several orders of magnitude more risk-averse than the supplier and, therefore, wants to protect herself from performance risk with a very large inventory. In most of our numerical examples, which cover a wide range of parameter combinations, the customer’s objective function is, indeed, increasing monotonically in  $s$ . Therefore, we will henceforth assume that the problem parameters are such that the backorder constraint is binding, so the optimal inventory position  $s^{SB}$  satisfies  $E[B | s^{SB}] = \widehat{B}_0$ . Given that  $v$  is completely determined by  $\alpha$  and  $s$  according to (13), the only variable to be determined is the cost-sharing parameter  $\alpha$ , so our problem is simplified to a one-dimensional optimization.

**Lemma 1** *The customer’s Lagrangian (12) is convex in  $\alpha$  when  $s$  is fixed.*

It follows that there is a unique  $\alpha^{SB}$  that minimizes the customer’s objective function. A closed-form solution exists, but it is quite complex (see the proof in the accompanying Technical Appendix, Kim et al. [17]) and inspection alone does not provide ready insights. Instead, we focus on understanding

how the parameters of the contract change when cost uncertainty  $\text{Var}[\varepsilon]$  changes. There are several motivations behind this analysis. First, cost uncertainty is of primary importance in practice because it is often harder to estimate than performance uncertainty. Second, over the product life cycle, significant changes occur in cost uncertainty (while performance uncertainty can be relatively more stable), so understanding how contractual terms should change in response becomes necessary. Finally, as will be seen shortly, by varying cost uncertainty we are able to obtain insights that, under some conditions, differ fundamentally from insights in the classical literature on moral hazard problems with multitasking.

**Proposition 5** *Suppose  $r_0, r > 0$  and that  $s^{SB}$  is fixed by the backorder constraint  $E[B | s^{SB}] = \widehat{B}_0$ . Then  $\alpha^{SO} < \alpha^{SB} < \alpha^{AO}$  and  $v^{SB} > v^{AO} > v^{SO} = 0$ . Further, let  $\ell(r_0, r) = \partial \mathcal{L} / \partial \alpha|_{\alpha=\alpha^{FB}}$  where  $\mathcal{L}$  is the customer's Lagrangian defined in (12). Function  $\ell(r_0, r)$  increases in the ratio  $r/r_0$  and crosses zero exactly once. The optimal contract parameters  $\alpha^{SB}$  and  $v^{SB}$  are related to  $\alpha^{FB}$  and  $v^{FB}$  as follows.*

- (i) *If  $\ell(r_0, r) > 0$ ,  $\alpha^{SB} < \alpha^{FB}$ ,  $d\alpha^{SB}/d(\text{Var}[\varepsilon]) > 0$ , and  $dv^{SB}/d(\text{Var}[\varepsilon]) < 0$ .*
- (ii) *If  $\ell(r_0, r) = 0$ ,  $\alpha^{SB} = \alpha^{FB}$ ,  $v^{SB} = v^{FB}$ , and  $d\alpha^{SB}/d(\text{Var}[\varepsilon]) = dv^{SB}/d(\text{Var}[\varepsilon]) = 0$ .*
- (iii) *If  $\ell(r_0, r) < 0$ ,  $\alpha^{SB} > \alpha^{FB}$ ,  $d\alpha^{SB}/d(\text{Var}[\varepsilon]) < 0$ , and  $dv^{SB}/d(\text{Var}[\varepsilon]) > 0$ .*

First, we note that the optimal cost sharing ratio  $\alpha^{SB}$  is bounded above by  $\alpha^{AO}$ , the optimal ratio when the cost reduction effort  $a$  is observable. In the current case the effort is not observable and therefore the customer has to reduce  $\alpha$  to provide more incentives to reduce costs. The side effect is that the supplier's effective unit cost  $(1 - \alpha)c$  increases, thus requiring a higher performance incentive  $v$  to induce the desired inventory position  $s^{SB}$ . Therefore,  $v^{SB} > v^{AO}$ . Second, we note that  $\alpha^{SB}$  is bounded below by  $\alpha^{SO}$ , which we derived by assuming that the inventory position  $s$  is observable. When  $s$  is not observable, the customer needs to provide a higher performance incentive,  $v^{SB} > v^{SO} = 0$ . But doing so exposes both the customer and the supplier to performance risk (recall the performance risk premium is increasing in  $v$  for both the customer and the supplier; see (4) and (5)), thus creating inefficiency that can be mitigated by increasing  $\alpha$ . Higher  $\alpha$  reduces the effective unit cost  $(1 - \alpha)c$  for the supplier and allows him to achieve the inventory position  $s^{SB}$  with a smaller  $v$ . Hence, increasing  $\alpha$  above  $\alpha^{SO}$  is optimal.

A comparison of the second-best solution with the first-best solution is more complex. It is instrumental to consider two cases based on the relative risk aversion of the customer and the supplier separately. Since function  $\ell(r_0, r)$  increases in the ratio  $r/r_0$  and crosses zero exactly once, the condi-

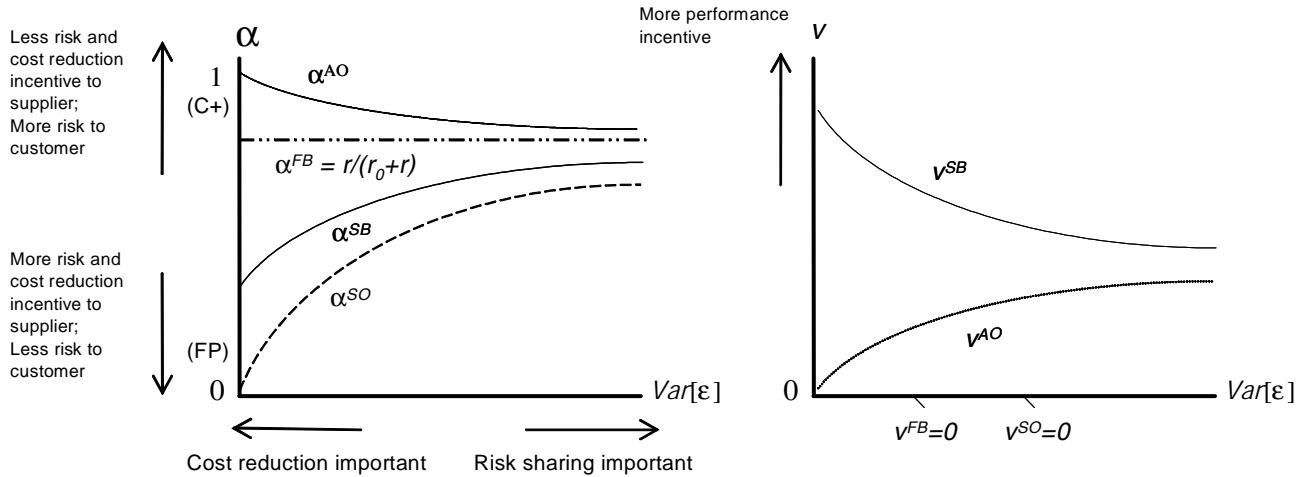


Figure 2: Optimal contract parameters as a function of  $\text{Var}[\varepsilon]$  when the supplier is relatively more risk-averse than the customer ( $\ell(r_0, r) > 0$ ).

tion  $\ell(r_0, r) > 0$  in (i) can be interpreted as  $r \succ r_0$ , where the symbol “ $\succ$ ” means that the supplier is relatively more risk-averse than the customer. Similarly,  $\ell(r_0, r) < 0$  can be interpreted as  $r \prec r_0$ , whereby the customer is relatively more risk-averse than the supplier. We first consider the former situation (which may arise if the customer is a bigger and more diversified company than the supplier). We believe that this case is more natural in practice. Figure 2 illustrates the results in (i).

We make the following observations from these figures. First,  $\alpha^{SB} < \alpha^{FB}$ , and the unobservability of effort and inventory results in less cost reimbursement than under the first-best solution. Second,  $\alpha^{SB}$  increases with  $\text{Var}[\varepsilon]$  and asymptotically approaches  $\alpha^{FB}$ . With large cost uncertainty, the risk-averse supplier is reluctant to participate in the trade, so the customer has to provide insurance by reimbursing a large proportion of the supplier’s costs. Thus the supplier has less incentive to make efforts to reduce costs. On the other hand, when  $\text{Var}[\varepsilon]$  is small, providing cost-reduction incentives becomes more important. Third, the gap between  $\alpha^{SB}$  and  $\alpha^{SO}$  decreases in  $\text{Var}[\varepsilon]$ . This gap can be interpreted as the additional inefficiency attributed to performance risk. When cost uncertainty is large, performance uncertainty  $\text{Var}[B | s^{SB}]$  is negligible and the gap between SB and SO disappears. The gap between  $\alpha^{SB}$  and  $\alpha^{AO}$  is interpreted similarly. Finally,  $v^{SB}$  decreases with  $\text{Var}[\varepsilon]$ , asymptotically approaching  $v(\alpha^{FB}, s^{FB})$ . With higher cost uncertainty, the performance incentive is lowered.

Overall, we observe that  $\alpha^{SB}$  and  $v^{SB}$  move in the opposite directions as  $\text{Var}[\varepsilon]$  increases because the customer increases  $\alpha$  to mitigate the supplier’s cost risk (we recall that the supplier is more risk-averse than the customer in the current setting). As a result, the supplier’s effective unit cost  $(1 - \alpha)c$

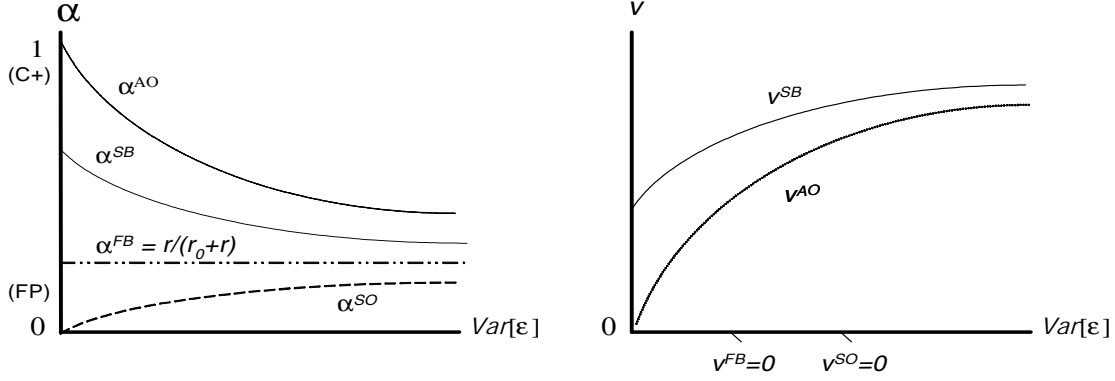


Figure 3: Optimal contract parameters as a function of  $\text{Var}[\varepsilon]$  when the customer is relatively more risk-averse than the supplier ( $\ell(r_0, r) < 0$ ).

is smaller, making it less expensive to stock inventory and allowing for a smaller incentive  $v$ . Therefore increasing  $1 - \alpha$  has the same effect on inventory as increasing  $v$ ; these two incentives are *complements* with respect to  $s$ .

This conclusion is similar to the one presented in Holmström and Milgrom’s [15] original multitask principal-agent model in which increasing variability in one output leads to weaker incentives for all outputs. Yet, the mechanism by which we arrive at our conclusion is different. Specifically, in Holmström and Milgrom [15], raising one effort raises the marginal disutility of raising another effort, which is not the case in our model (since the supplier’s disutilities  $(1 - \alpha)cs$  and  $ka^2/2$  are independent of each other). Another important assumption in their model is that the outcomes are affected by exactly one effort each, so there is a one-to-one correspondence between an incentive and an effort. In contrast, our model has an outcome  $C$  that is a function of both variables  $a$  and  $s$  via  $C = cs - a + \varepsilon$ . In this respect, the model closest to ours is found in Bolton and Dewatripont ([2], pp. 223-8) where there is *direct conflict between the tasks*, because exerting one effort positively affects one outcome but negatively affects the other.

Next, we consider the case in which the customer is relatively more risk-averse than the supplier,  $r < r_0$  (case (iii) in Proposition 5). Figure 3 is an analog of Figure 2. Compared to the previous discussion,  $\alpha^{SB}$  and  $v^{SB}$  exhibit exactly opposite behavior. Now  $\alpha^{SB} > \alpha^{FB}$  and  $\alpha^{SB}$  decreases in  $\text{Var}[\varepsilon]$  while  $v^{SB}$  increases in  $\text{Var}[\varepsilon]$ . This fundamental difference arises because, unlike in the previous case, the customer now needs more protection from cost risk. In the presence of large cost uncertainty, this can be achieved by choosing small  $\alpha$ , thereby transferring most of the risk to the supplier. A

nonintuitive consequence of this outcome is that the supplier is incentivized more to reduce his cost and increase his stocking level when cost uncertainty is great. Therefore, the customer’s concern for her own risk protection reverses contractual terms and comparative statics. The complementarity between  $1 - \alpha^{SB}$  and  $v^{SB}$  still remains, however: as  $1 - \alpha^{SB}$  increases, so does  $v^{SB}$ . We note that results when the customer is more risk-averse than the supplier are somewhat contrary to what we have come to expect from the existing literature on multitasking where the customer is often assumed to be risk-neutral.

## 6 Example with Multiple Risk-Averse Suppliers

In this section we present a numerical analysis of the problem with multiple suppliers. We illustrate our findings through an example based on real-life maintenance data from a fleet of military fighter aircraft. This example shows how our model can be applied in practice to support long-term strategic planning and contract negotiations (note that we also considered a simpler case where there are two suppliers that differ by at most one of the parameters  $\{r_i, \text{Var}[\varepsilon_i]\}$ , thereby isolating the trade-off between incentives and risk; see Kim et al. [17])

A total of  $N = 156$  aircraft are deployed in the fleet. We obtained data on unit costs, daily failure rates, and repair lead times for a representative collection of 45 line replaceable units (“parts”) that are unique to the aircraft and covered by a PBL contract. To utilize our model we aggregate data into five subsystem groups: avionics (a), engines (e), landing gear (l), mechanical (m), and weapons (w), based on descriptions of each part. We employ the following technique to obtain unit costs, failure rates, and lead times for these subsystems. First, we assign each part to one of the groups, and compute the subsystem’s mean inventory on-order as  $\mu_i = \sum_{j=1}^{n_i} \lambda_j L_j$ , where  $i = \{a, e, l, m, w\}$  and  $n_i =$  the number of parts within subsystem  $i$ . Thus, we treat each subsystem as a “kit” which is replaced whenever any part within it fails. Subsystem unit costs are inferred from an output generated by the proprietary commercial software from MCA Solutions, Inc. (<http://www.mcasolutions.com>). Given a system availability target, this software calculates optimal stocking levels over multiple echelons and indentures while directly considering each part-location. By aggregating its output, we can infer the effective subsystem unit costs by dividing the dollar amount invested in inventory resources for each subsystem ( $\sum_{j=1}^{n_i} c_j s_j$ ) by the total number of stocking units within it ( $\sum_{j=1}^{n_i} s_j$ ). For this example the availability target of 95% was chosen. Table 2 summarizes the inferred values of  $\{\mu_i\}$  and  $\{c_i\}$

Subsystem	avionics (a)	engine (e)	landing gear (l)	mechanical (m)	weapons (w)
$\mu_i$	10.46	19.36	13.72	16.87	8.43
$c_i$ (in \$1,000)	21.52	6.60	31.08	8.52	14.85

Table 2:  $\mu_i$  and  $c_i$  for each subsystem.

$i$	$\rho_i = 0.02$					$\rho_i = 0.1$				
	a	e	l	m	w	a	e	l	m	w
$\alpha_i^{SB}$	0.54	0.67	0.88	0.41	0.51	0.63	0.35	0.92	0.48	0.75
$v_i^{SB}$	5.77	8.11	1.46	6.49	4.35	5.01	12.61	1.14	5.97	3.06
$a_i^{SB}$	99.74	21.66	38.15	50.58	73.10	79.14	43.11	25.01	44.04	37.52
$s_i^{SB}$	9.29	23.12	10.51	19.26	8.66	9.35	22.77	10.39	19.27	8.96
$\hat{A}_i$	98.75%	99.69%	97.69%	99.54%	99.33%	98.77%	99.65%	97.63%	99.54%	99.42%
IIR $_i$	200.0	152.6	326.8	164.1	128.6	201.2	150.3	322.9	164.2	133.1
NCR $_i$	76.6	18.1	35.8	35.6	55.1	64.6	29.0	24.0	32.7	32.8
CRP $_i$	23.4	1.5	68.6	2.8	17.6	557.3	15.1	1669.3	68.1	318.8
PRP $_i$	35.9	10.0	19.8	15.9	16.1	26.7	28.2	12.2	13.4	7.0

Table 3: Optimal contract terms and suppliers' actions. The dollar figures are in thousands. IIR stands for investment in resources and is equal to  $c_i s_i^{SB}$ . NCR is  $-a_i^{SB} + \frac{1}{2} k_i (a_i^{SB})^2$ , the net cost reduction. CRP is the residual cost risk premium,  $\frac{1}{2}(r_0(\alpha_i^{SB})^2 + r_i(1 - \alpha_i^{SB})^2)\text{Var}[\varepsilon_i]$ , and PRP is the residual performance risk premium,  $\frac{1}{2}(r_0 + r_i)(v_i^{SB})^2\text{Var}[B_i | s_i^{SB}]$ . System availability target is 95%.

using this heuristic.<sup>7</sup> We note that  $\{\mu_i\}$  are an order of magnitude smaller than  $N$ , thus satisfying the condition  $E[B_i | s_i] \ll N$  needed to apply the fixed failure rate approximation.

To determine values of parameters  $\{k_i\}$  and  $\{\text{Var}[\varepsilon_i]\}$ , we use the following approach. Let  $K_i$  be the supplier  $i$ 's fixed cost such that  $K_i = E[K_i] + \varepsilon_i$ . For each supplier, we assume that the expected fixed cost is 50 times higher than the unit cost  $c_i$ . The maximum dollar amount of cost reduction  $a_i^{FB} = 1/k_i$  is assumed to be  $0.2E[K_i]$ . Thus,  $k_i = 1/(10c_i)$ . For the sake of simplicity, we also assume that the coefficient of variation  $\rho_i \equiv \sqrt{\text{Var}[K_i]}/E[K_i]$  is the same across suppliers. We infer the risk aversion coefficient for each supplier from the market capitalization of a representative manufacturer of such a subsystem. For example, if Boeing is chosen as the customer and GE as the engine supplier, we calculate the risk aversion ratio of  $r_0/r_e \simeq 7$  since GE's market capitalization is roughly 7 times that of Boeing (see justification for using company size as a proxy for risk aversion in Cummins [9]). This approach is, of course, quite simplistic, but it fits our aim to illustrate the model. Using this methodology, we choose  $r_a/r_0 = 1.79$ ,  $r_e/r_0 = 0.15$ ,  $r_l/r_0 = 11.76$ ,  $r_m/r_0 = 1$ , and  $r_w/r_0 = 3.33$ , and we select  $r_0 = 0.15$ . The optimal contract terms and the suppliers' actions are presented in Table 3.

We consider two scenarios: with small and high cost uncertainty (as captured by the coefficient of variation  $\rho_i$ ). For simplicity, assume that all suppliers have the same value of  $\rho_i$ . Table 3 summarizes

<sup>7</sup>Note that our data are restricted to the subset of unique parts under a PBL contract. Consequently the inferred values of  $\{\mu_i\}$  and  $\{c_i\}$  are not representative of the values associated with all of the parts used to support the subsystem.

optimal contract parameters and the implied cost terms, including the cost and performance premiums. In the case of high uncertainty, observe that the cost premium is higher than the performance premium for all suppliers except for the engine supplier (e). This asymmetry arises because he is the only supplier who is less risk averse than the customer. On the other hand, the performance premium becomes more salient when cost uncertainty is small. We also observe that  $\{\alpha_i^{SB}\}$  increases and  $\{v_i^{SB}\}$  decreases with  $\rho_i$  for all suppliers except (e), which is consistent with our results for a single supplier. Finally, the values of  $\{s_i^{SB}\}$  are quite insensitive to changes in  $\rho_i$  as noted in the previous example.

## 7 Conclusion

The goal of this paper is to introduce contracting considerations into the management of after-sales service supply chains. We do so by blending the classical problem of managing the inventory of repairable service parts with a multitask principal-agent model. We use this model to analyze incentives provided by three commonly used contracting arrangements, fixed-price, cost-plus, and performance-based (FP, C+ and PBL). By doing so, we analyze two practically important issues of contracting in service supply chains – performance requirement allocation and risk sharing – when a single customer is contracting with a collection of first-tier suppliers of the major subsystems used by an end product/system. When performance is defined as overall system availability, the answer to the former can be found from the solution of the classic service part resource allocation problem. Our innovation is in explicitly modeling decentralized decision making and considering how firms behave when they face uncertainties arising from both support costs and product performance. The notion of risk sharing found in the principal-agent literature is incorporated into our model, providing insights into what types of contracts should be used under various operating environments. Specifically, we have discovered that incentive terms in the contract exhibit complementarity, i.e., incentives for both cost reduction and high availability move in the same direction as cost uncertainty changes.

Furthermore, our analysis allows us to make normative predictions with respect to how contracts are likely to evolve over the product life cycle. In our model, we assumed that supplier effort reduces support costs but does not improve product performance reliability or repair capabilities. This is consistent with the observation that performance uncertainty is relatively stable throughout the repair and maintenance process, while cost uncertainty is likely to be reduced over time by learning about costs through the deployment of a larger fleet of systems. Thus, if a series of performance contracts

are signed over the product lifetime, our analysis indicates that the cost reimbursement ratio  $\alpha$  will decrease (increase) over time if the supplier is relatively more (less) risk-averse than the customer. For the performance incentive  $v$  the direction is reversed. Since larger, more diversified customers are more common in practice, our results predict that the optimal contract will typically assume less cost sharing and more performance incentive as the product matures. Indeed, this prediction is confirmed by practitioners and from the DoD publications: “PBL strategies will generally have a phased contracting approach, initiated by Cost Plus cost reimbursement type contracts to Cost Plus incentive contracts to Fixed Price incentive contracts, over time” (Defense Acquisition University [13]).

We find that, in the presence of great residual uncertainty associated with performance, cost sharing is still an effective tool even if cost uncertainty is small. That is, the combination FP/performance-based contract is not optimal in such instances (notice the gap between zero and  $\alpha^{SB}$  at  $\text{Var}[\varepsilon] = 0$  in Figure 2), because the cost reimbursement  $\alpha$  can be used as a risk protection mechanism even for the risk borne by the performance. While inventory  $s$  can be used as an instrument to hedge against performance risk, adjusting  $\alpha$  is more effective for this purpose because the primary role of  $s$  is controlling for the backorder level in order to achieve the availability target. Hence, some degree of cost sharing is recommended in a performance contracting environment even when cost uncertainty is low. Our numerical study shows that the optimal inventory position profile  $\{s_i^{SB}\}$  is quite insensitive to changes in risk-related parameters such as  $r_0$ ,  $r_i$ , and  $\text{Var}[\varepsilon_i]$ . This happens because the presence of a stringent backorder constraint limits the range in which  $\{s_i^{SB}\}$  can be varied.

Performance-based contracting in service supply chains offers fertile ground for research where economics and classical inventory theory converge naturally. Not only does it pose theoretically challenging questions, but insights gained from the analysis are of great interest to practitioners who are currently undergoing major business process changes due to the move towards PBL contracting. Our paper analyzes several major issues in performance contracting, but many open questions remain. Follow-up studies may address such topics as the free-riding problem arising from overlapping downtimes across parts; gaming among suppliers and the consequences to realized performance; long-term, strategic product reliability investment vs. intermediate-term, tactical inventory decisions; investment in enhanced repair and logistics capabilities that would reduce lead times; alternative ownership and management scenarios; and many more. We are currently working on some of these issues (for example, see Kim et al. [18]) Finally, empirical verification of the insights gained from this paper will lead to more effective implementation of contract design and aid contract negotiations.

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